

Article

Information Transfer in Active States of Human β_2 -Adrenergic Receptor via Inter-Rotameric Motions of Loop Regions

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Featured Application: Loop regions in β_2 AR are critical hot spot regions, likely in other GPCRs, and can be used as potential allosteric drug targets.

Abstract: Two independent 1.5 μ s long MD simulations were conducted for the fully atomistic model of the human beta2-adrenergic receptor (β_2 AR) in a complex with a G protein to investigate the signal transmission in a fully active state via mutual information and transfer entropy based on α -carbon displacements and rotameric states of backbone and side-chain torsion angles. Significant correlations between fluctuations in α -Carbon displacements were mostly detected between transmembrane (TM) helices, especially TM5 and TM6 located at each end of ICL3 and TM7. Signal transmission across β_2 -AR was quantified by shared mutual information; a high amount of correspondence was distinguished in almost all loop regions when rotameric states were employed. Moreover, polar residues, especially *Arg*, made the most contribution to signal transmission via correlated side-chain rotameric fluctuations as they were more frequently observed in loop regions than hydrophobic residues. Furthermore, transfer entropy identified all loop regions as major entropy donor sites, which drove future rotameric states of torsion angles of residues in transmembrane helices. Polar residues appeared as donor sites from which entropy flowed towards hydrophobic residues. Overall, loops in β_2 AR were recognized as potential allosteric hot spot regions, which play an essential role in signal transmission and should likely be used as potential drug targets.

Keywords: transfer entropy; rotameric state; loop region; allosteric network; mutual information

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1. Introduction

Allostery is an essential property of all proteins that is accepted to be intrinsic, irrespective of their functional requirements [1,2]. In fact, all proteins are dynamic entities, which sample distinct conformational states, and allostery is manifested as the shift in that conformational ensemble when one site of a protein is triggered by either a bound ligand or a mutation. In some proteins, the catalytic region at a distant site experiences a change in its functional capacity; thus, allostery becomes a critical part of the protein's functional regulation [2–4]. In addition to conformational changes, allostery can also manifest itself as a change in the global dynamics of the protein. Based on Cooper and Dryden's model proposed almost 30 years ago, allostery arises from the changes in frequencies and amplitudes of thermal fluctuations even in the absence of any conformational change in the backbone [5]. In this entropic model of allostery, there is no redistribution in the preexisting conformational substates. However, there is a change in the depth of the corresponding local minima in which a coordinated fluctuation of residues transmits the change from one site to another distant site [6–8].

Another important aspect of allostery is the pathway along which the residues fluctuating in the correspondence are distributed. These so-called “hot spot” residues are essential for site-to-site communication and are valuable for computer-aided drug design

studies as they often provide high specificity/selectivity in comparison to orthosteric binding site residues, which are mostly conserved among species [9–14]. Over the years, several graph-based algorithms have been developed to estimate this functional allosteric circuit with its constitutive residues [15–17]. Here, we used correlated fluctuations between residues to establish an allosteric communication network, which is described in terms of entropy/information transfer from one site to another. Transfer entropy was previously introduced by Schreiber in 2000 as an information-theoretic measure to quantify the exchange of information between two systems [18] and was later used in several MD studies as an analysis tool to understand the effects of various structural changes [19–23].

In our current study, the transfer information of coupled fluctuations was not only based on translational $C\alpha$ displacements, as often considered in several studies, but also on rotational displacements of backbone and side-chain torsion angles in each residue. The thermodynamic importance of side-chain variability was previously emphasized in calmodulin-ligand binding studies [24,25]. Furthermore, NMR mutational studies demonstrated the contribution of side-chain fluctuations to long-range communication networks [26]. Previously, using Monte Carlo sampling, DuBay and his coworkers demonstrated that allosteric communication in proteins can be transmitted by correlated side-chain fluctuations only [27]. However, they assumed a fixed backbone rotation and quantified the correspondence using a mutual information metric only. Here, our study will be the first to consider both backbone and side-chain rotatable bonds altogether to identify the correlated fluctuations in the rotameric states of these torsion angles. In addition, we will use another information-theoretic measure, the so-called “transfer entropy” to determine the dynamics of information transport, i.e., the direction of the exchange of information from one site to another distant site in the receptor at a future time.

The system under study is a human beta2-adrenergic receptor (β_2 AR) in complex with G protein representing the active state. It was subjected to two separate 1.5 μ s long MD simulations, which amounted to a 3 μ s long trajectory. Dynamic cross-correlation analysis based solely on α -Carbon displacements was followed by mutual information and transfer entropy calculations based on fluctuations in both α -Carbon displacements and rotameric state of backbone and side-chain rotatable bonds. A significant amount of correspondence was observed for fluctuations in rotameric states for residues in loop regions. This overlooked information carried via fluctuations within the rotameric well was emphasized for the first time in this study as an important component of allosteric regulation. Furthermore, the information transfer was directed from polar residues located in loop regions towards hydrophobic residues found in the transmembrane regions of the receptor, i.e., fluctuations in rotameric states of polar loop residues dictated the future fluctuations of rotameric states of hydrophobic transmembrane residues. This driver–follower relation between the loop and transmembrane regions of the receptor via polar/hydrophobic residue pairs elucidated for the first time an important allosteric communication network that can be used for allosteric drug design studies.

2. Materials and Methods

System Preparation. The active state of human β_2 AR in a complex with a Gs complex and bound to agonist BI-167107 with a PDB id of 3SN6 [28] was used as an initial state conformation for MD simulations. Prior to the runs, T4 Lysozyme, nanobody, and the agonist were removed, the missing extracellular (*Ala176-His178*) and intracellular (*Phe239-Phe265*) residues were completed via a MODELLER homology modeling tool [29], and the mutations T96M, T98M and E187N, which were used as linkers in crystal structure formation were reverted to their original state via the *mutate* plugin of the VMD visualization tool [30]. The system was then embedded into a palmitoylcholine (POPC) lipid bilayer using VMD’s *membrane* plugin tool [30], solvated with TIP3P water molecules, and later ionized with 160 Na^{+2} and 154 Cl^{-1} counter ions for neutralization, which is necessary for the Particle-Mesh Ewald summation method. The system with the dimensions of $125 \times 125 \times 165 \text{ \AA}$ was prepared with a total of 228,299 atoms, of which 54,707 were

water molecules. The CHARMM36 forcefield was used to describe the interaction potential of protein and lipids [31]. Periodic boundary conditions were applied in an isothermal, isobaric NPT ensemble with a constant temperature of 310 K and a constant pressure of 1 bar. Temperature and pressure were controlled by the Langevin thermostat and Langevin piston barostat, respectively [32]. The equations of motion were integrated with a 2 fs time step, and the SHAKE algorithm was used to constrain covalent bonds involving non-water hydrogen bonds with a non-bonded cutoff value of 12 Å.

Two independent 1.5 μs long MD runs were performed via the NAMD v2.13 software tool. Each run was initiated with three steps of initial energy minimizations under flexible cell conditions, including (i) the melting of lipid tails when the rest of the atoms were fixed, (ii) minimization and equilibration when protein was constrained but lipid, water, and ion atoms were released, and (iii) minimization and equilibration with the release of all atoms, which was then followed by equilibrium and production runs under constant area according to the membrane proteins' simulation protocol of NAMD [33]. The lipid bilayer in the system was continuously monitored in the minimization and equilibration steps until reaching 63.69 Å² area per lipid ratio, which was in the range of the experimentally reported value of 64.3 ± 1.3 Å² [34,35].

Dynamic Cross-Correlation. Correlations between atomic fluctuations from average positions of two residues i and j were calculated using the following equation:

$$C_{i,j} = C(\Delta R_i, \Delta R_j) = \frac{\langle \Delta R_i(t) \cdot \Delta R_j(t) \rangle}{\sqrt{\langle (\Delta R_i)^2 \rangle \langle (\Delta R_j)^2 \rangle}} \quad (1)$$

The time average of the dot product of $\Delta R_i(t)$ and $\Delta R_j(t)$ was taken and normalized. $\Delta R_i(t)$ and $\Delta R_j(t)$ represent the atomic fluctuations of α -Carbons only. If $C_{ij} = 1$, then the fluctuations of atoms i and j are perfectly correlated (fluctuates in the same direction), if $C_{ij} = -1$, then the fluctuations of atoms i and j are perfectly anticorrelated (fluctuates in opposite directions), and if $C_{ij} = 0$, then the atoms i and j fluctuate independently.

Contact map generation. The cutoff distance (R_c) for heavy atoms (C, N, O, S) was taken as 6 Å, below which the atoms were considered to be in contact. The incorporation of all heavy atoms provides a more accurate representation of the contact profile than that of α -Carbons only. The formula used for contact map calculation was defined as:

$$M_{i,j} = \begin{cases} 1, & \text{if } \delta_{i,j} \leq R_c \\ 0, & \text{Otherwise} \end{cases} \quad (2)$$

Contact percentages over the MD trajectory were calculated with $\sum_{n=1}^{nconf} M_{i,j} / nconf$ and the threshold was set to 75% of the whole trajectory to recognize stable contacts.

Mutual Information (MI). Mutual information based on α -Carbon positional fluctuations between residue pairs i and j was calculated using the following expression:

$$MI(i, j) = \sum_k p(\Delta R_i(t_k), \Delta R_j(t_l)) \log_2 \frac{p(\Delta R_i(t_k), \Delta R_j(t_l))}{p(\Delta R_i(t_k)) \cdot p(\Delta R_j(t_l))} \quad (3)$$

where $p(\Delta R_i(t_k), \Delta R_j(t_l))$ represents the joint probability of observing the fluctuation of residue i in state k and that of residue j in state l . Mutual information is a non-negative and symmetric quantity, and zero if the fluctuations of residue i are independent of the fluctuations of residue j . To calculate the probability of occurrence, $p(\Delta R_i(t_k), \Delta R_j(t_l))$, the number of states k and l , also described as the number of bins, N_{bins} , were determined for each residue separately using Shannon's entropy criterion. The number of bins (or states)

for each residue was determined as the value for which Shannon's entropy reaches its maximum. The convergence criterion was expressed as:

$$\frac{|H(N_{bins} + 1)_i - H(N_{bins})_i|}{H(N_{bins})_i} < 0.02 \quad (4)$$

where $H(N_{bins})_i$ is the Shannon entropy for residue i with N_{bins} . Similarly, mutual information based on fluctuations in backbone and side torsion angles were expressed as:

$$MI_{i,j} = \sum_{\Theta_i} \sum_{\Theta_j} p(\Theta_i, \Theta_j) \log_2 \left(\frac{p(\Theta_i, \Theta_j)}{p(\Theta_i) p(\Theta_j)} \right) \quad (5)$$

where $p(\Theta_i, \Theta_j)$ denotes the joint probability of observing the joint state (Θ_i, Θ_j) of residues i and j . Here, Θ_i and Θ_j represent the rotameric states of backbone φ , ψ and side-chain dihedrals χ_i , $i = 1, 2, 3, 4$ in residues i and j , respectively. Based on the distribution of rotameric states, the number of discrete rotameric states (or bins) for backbone dihedrals was set to 3, whereas for side-chain dihedrals, the number of states varied between 0 and 6 according to the rotamer library [36].

Transfer Entropy. Transfer entropy is defined as the reduction in uncertainty in future states of residue j at $t + \tau$ by knowing the states of residue i at time t . Based on Shreiber's work [18], it was defined by Erman et al. [22,23] as;

$$TE_{i \rightarrow j}(\tau) = H(\Delta R_j(t) | \Delta R_j(t - \tau)) - H(\Delta R_j(t) | \Delta R_j(t - \tau), \Delta R_i(t - \tau)) \quad (6)$$

where $H(\Delta R_j(t) | \Delta R_j(t - \tau))$ is the conditional entropy of residue j at time t given the values of ΔR_j at time $t - \tau$. The second term $H(\Delta R_j(t) | \Delta R_j(t - \tau), \Delta R_i(t - \tau))$ is the conditional entropy of residue j at time t given the values of ΔR_i and ΔR_j at time $t - \tau$. When entropies are expressed as a function of the probability of occurrences of positional fluctuations ΔR , $TE_{i \rightarrow j}(\tau)$ becomes,

$$TE_{i \rightarrow j} = -\langle \log_2 p(\Delta R_j(t), \Delta R_j(t - \tau)) \rangle + \langle \log_2 p(\Delta R_j(t - \tau)) \rangle + \langle \log_2 p(\Delta R_j(t), \Delta R_j(t - \tau), \Delta R_i(t - \tau)) \rangle - \langle \log_2 p(\Delta R_j(t - \tau), \Delta R_i(t - \tau)) \rangle \quad (7)$$

A similar expression for transfer entropy was used for rotameric states, where ΔR was replaced by Θ , which includes the information of the rotameric state of all rotatable sp^3 - sp^3 bonds in each residue (φ , ψ , χ_i , $i = 1, 2, 3, 4$). However, for a residue pair such as *Lys-Arg*, where both residues include four side-chain rotatable bonds, each having 3 alternative rotameric states, the joint probability $p(\Theta_j(t), \Theta_j(t - \tau), \Theta_i(t - \tau))$ is comprised of 3^{18} ($= 3^6 \times 3^6 \times 3^6$) different rotameric states. For a protein system with 312 residues, the calculation of the transfer entropy becomes computationally intractable as it exceeds the maximum size an array can hold. Thus, only the first side-chain rotameric state was considered together with two backbone torsion angles, i.e., (φ, ψ, χ_1) , which yielded 3^9 ($= 3^3 \times 3^3 \times 3^3$) different states per residue. Finally, the net transfer entropy was determined by taking the difference between TE from i to j and that from j to i as,

$$NetTE_{i \rightarrow j} = TE_{i \rightarrow j} - TE_{j \rightarrow i} \quad (8)$$

The source codes for both mutual information and transfer entropy calculations were written by the authors using C programming language and can be provided upon request.

3. Results and Discussion

The active state of the receptor was well preserved throughout the simulation. As all members of the G protein-coupled receptor (GPCR) superfamily, human β_2AR shares the 7TM structural motif, which consists of seven transmembrane-spanning alpha helices connected by loop regions at the intra- and extracellular sides of the membrane (See Figure 1a). Among other loop regions, the intracellular loop 3 (ICL3) plays a critical

role in the recognition of G proteins [28]. In addition, there exists an allosteric coupling between ICL3 and the extracellular regions of the receptor, which incorporate the orthosteric binding site [37–39]. Conformational changes observed at the intracellular part affect the extracellular part, specifically the binding site, which holds key residues such as *Asp113* on transmembrane helix 3 (TM3), *Ser203*, *Ser204*, *Ser207* on TM5, *Phe289*, *Asn293* on TM6, and *Asn312* on TM7.

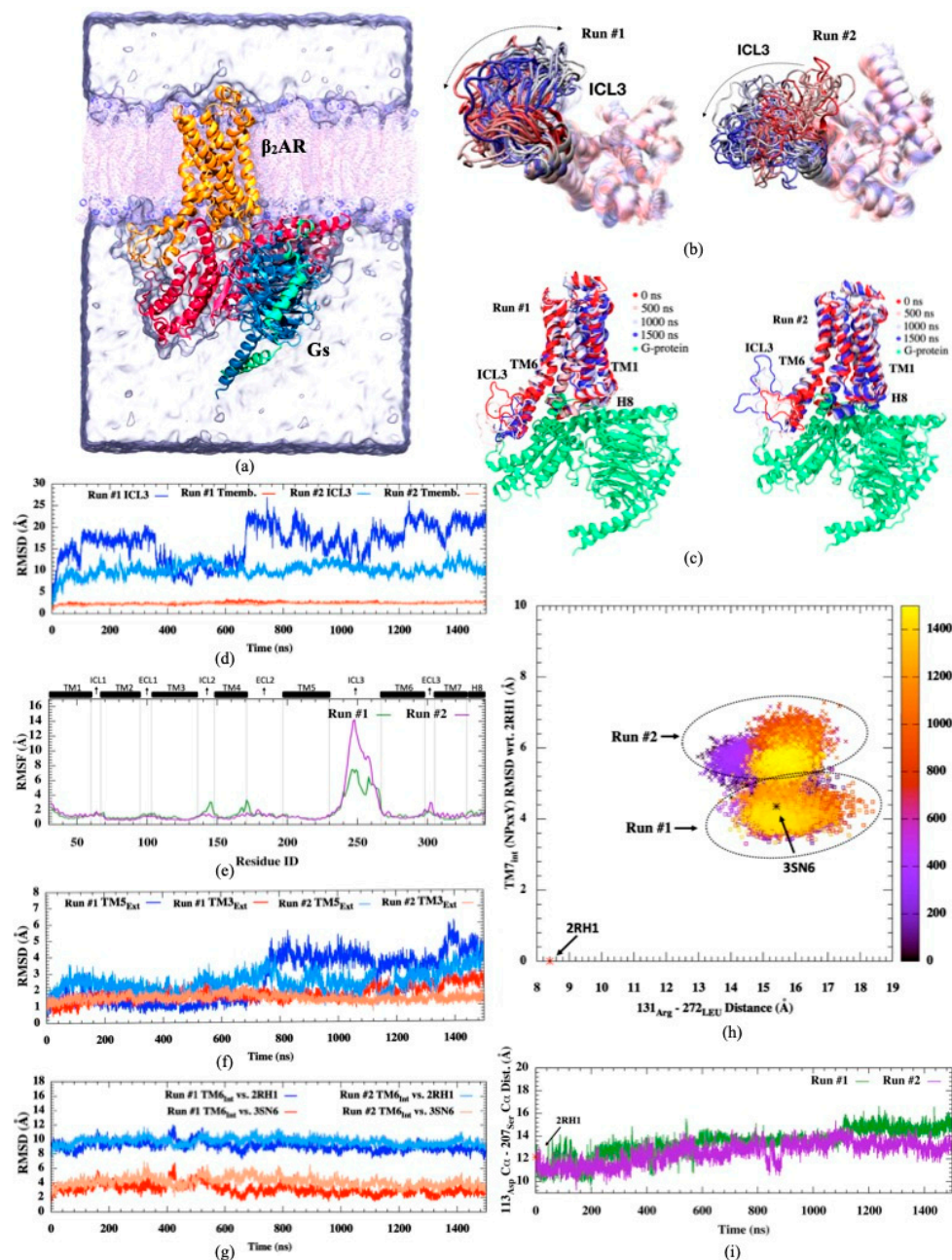


Figure 1. (a) Representation of human β_2 AR in a complex with Gs complex in a membrane environment (created via VMD visualization tool [30]), (b) Intracellular views of 20 snapshots of ICL3 (c) side views of β_2 AR-Gs complex for 4 different snapshots colored from red (initial) to white (intermediate), to blue (final) during simulation (d) RMSD profiles of ICL3 and transmembrane regions, (e) RMSF profiles (f) RMSD profile of extracellular parts of TM3 and TM5 helices, (g) RMSD profiles of intracellular parts of TM6, (h) RMSD of NPxxY motif of TM7 with respect to the inactive state (PDB id:2RH1) versus ionic lock distance (*Arg131C α -Leu272C α*), (i) distance profile for *Asp113C α -Ser207C α* residue pair.

The most important conformational changes observed in two independent runs were summarized in Figure 1. The active state of the receptor was well characterized by an approximately 11 Å outward movement in the cytoplasmic end of TM6, and consequently, the adjoining ICL3 was pushed aside towards the lipid molecules (See Figure 1a–c). This unique conformation of the active state was only preserved in the presence of a G protein, which displaces TM6 and ICL3 outward for easy access to the receptor's binding cavity. Aligned snapshots of the receptor indicated high mobility in ICL3 in both runs, slightly enhanced in the second run. RMSD profiles of transmembrane helices 3, 5, 6, and 7 (TM3, TM5, TM6, and TM7) indicated that their initial states were well preserved throughout the simulation within the boundaries characterizing the active state of the receptor (Figure 1d–h). On the other hand, the distance between α -Carbons of two key residues at the orthosteric binding site, *Asp113*, and *Ser207*, displayed a slight increase from a range of 10–12 Å up to 13–16 Å in both runs, especially more noticeable in Run #1 (See Figure 1i). Our simulations were conducted with no ligand attached at the orthosteric binding site. Thus, the increase in the distance between these two key residues clearly indicated the tendency of the cavity to expand a bit in the absence of any agonist attached, irrespective of the fact that the active state was well preserved throughout the receptor, especially at the G protein binding site.

Previously, we attempted to simulate the active state in its free form, i.e., its G protein partner removed (PDB id: 3SN6), and observed that the initially opened and swept away ICL3 region and its adjoining transmembrane helix 6 (H6) swiftly changed position towards the core of the receptor at the very early stages of the simulation (in the first 50 ns), closed itself towards the core of the receptor, and blocked the G protein binding cavity. Moreover, in a simulation study conducted by Ozgur et al. [37], bond restraints were employed at the orthosteric binding site to preserve certain key distances between TM3 and TM5 within the experimentally reported range that represented the active state. No G protein was attached, yet ICL3 preserved its initial open conformation as if there was a G protein nearby, although the TM6's upward tilt characterizing the active state was not observed. Clearly, the conformational state of the orthosteric binding site allosterically affects the conformational state of the distant G protein binding site. It might facilitate the opening of the cavity for the initial binding of G protein, yet the fully active state can only be achieved and preserved when there is a G protein nearby interacting with the receptor. In other words, the major conformational shift for the characteristic tilt in TM6 requires an energy boost that a G protein can only provide and thus cannot be achieved in the course of an MD simulation, which is confined to low energy conformational states. Moreover, the absence of an agonist, which is accompanied by only a slight expansion at the unoccupied orthosteric binding site, does not destabilize the active state, which is already securely preserved by a G protein.

Cross-correlations between α -Carbon displacements disclosed TM6 as the dominating site fluctuating in concert with the rest. It is important to highlight distant regions that display positional fluctuations that are correlated with each other, as they might indicate the presence of some potential sites in communication along the allosteric pathway. Thus, the contact map was overlaid with the residue-pair cross-correlation map, as depicted in Figure 2. The contact map was generated by using the heavy atoms with a threshold distance of 6 Å. Distant and correlated regions were mainly detected in the second half of the receptor composed of TM5, TM6, ICL3, TM7, and its small extension H8, especially TM6, which incorporated most critical sites for binding intracellular G proteins and small extracellular molecules. Especially, *Phe289*, *Asn293* on TM6, and *Asn312* on TM7, which are known to be key residues interacting with the ligand at the orthosteric site, fluctuated in the same direction, with ICL3 having correlation values as high as 0.8. Another set of critical residues at the orthosteric binding sites *Ser203*, *Ser204*, and *Ser207* located at the extracellular part of TM5 negatively correlated with the distant helical segment TM7 with a C_{ij} value of around -0.5 . Specifically, it is interesting to observe both *Ser203* and *Ser207*

on one side of the binding cavity fluctuating in opposite directions with *Asn312* on the opposite side.

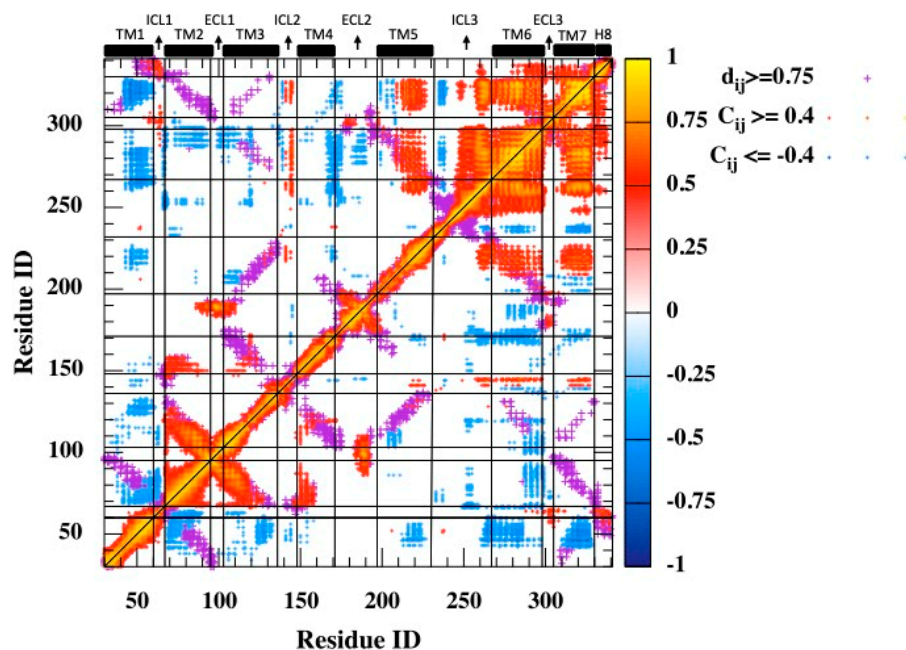


Figure 2. Residue-pair cross-correlation map for 3 μ s MD trajectory. Only $C_{ij} > +0.4$ and $C_{ij} < -0.4$ are represented. Magenta dots represent the contact map (threshold distance of 6 \AA).

Moreover, ICL2, the second-most important intracellular loop after ICL3, distantly fluctuated in concert with the second half of the receptor (TM5–H8). Finally, the first trans-membrane helix TM1, which incorporated the free amino-terminal tail, mostly fluctuated in the opposite direction from the rest of the receptor, especially the distant helices TM6, TM7, and to some extent with TM3 and TM5, which all incorporated critical key residues at the orthosteric binding site.

Rotamer-based mutual information is mostly observed between loop regions and shared among polar residues. Cross-correlation is a metric that ignores the correlated motions in orthogonal directions. Therefore, even perfectly correlated motions important for allosteric signaling may be overlooked if the positional fluctuations are perpendicular to one another. On the other hand, mutual information, a metric in information theory, determines the correspondence between fluctuations of residue pairs, irrespective of their directions. MI was first calculated for the positional fluctuations of backbone $C\alpha$ atoms, and as anticipated, the highest MI values (max. 4.01) were observed for residues close in space (see the diagonal line in Figure 3a). In addition, it is important to recognize high MI values observed between spatially distant residues as they would likely indicate the existence of an allosteric communication network, which is usually characterized by distant regions with a high degree of correspondence. As depicted in Figure 3a, mutual information was plotted together with a contact map to unravel the long-distance coupled motions of the allosteric network (see magenta dots). However, the only significant correspondence in distant $C\alpha$ fluctuations was detected between a few residues located in ICL3's midpoint and the distant extracellular parts of TM6, extracellular loop 3 (ECL3), and TM7, which incorporate critical orthosteric binding site residues such as *Phe289*, *Asn293*, and *Asn312*. It is obvious that mutual information between backbone atomic fluctuation was mostly shared by neighboring residues either close in sequence or space. For all MI maps in Figure 3, red dots represent MI values greater than 0.5, and green dots represent MI between 0.25 and 0.5. Any MI less than 0.25 was not displayed. For clarity, the contact map was illustrated in Figure 3a only.

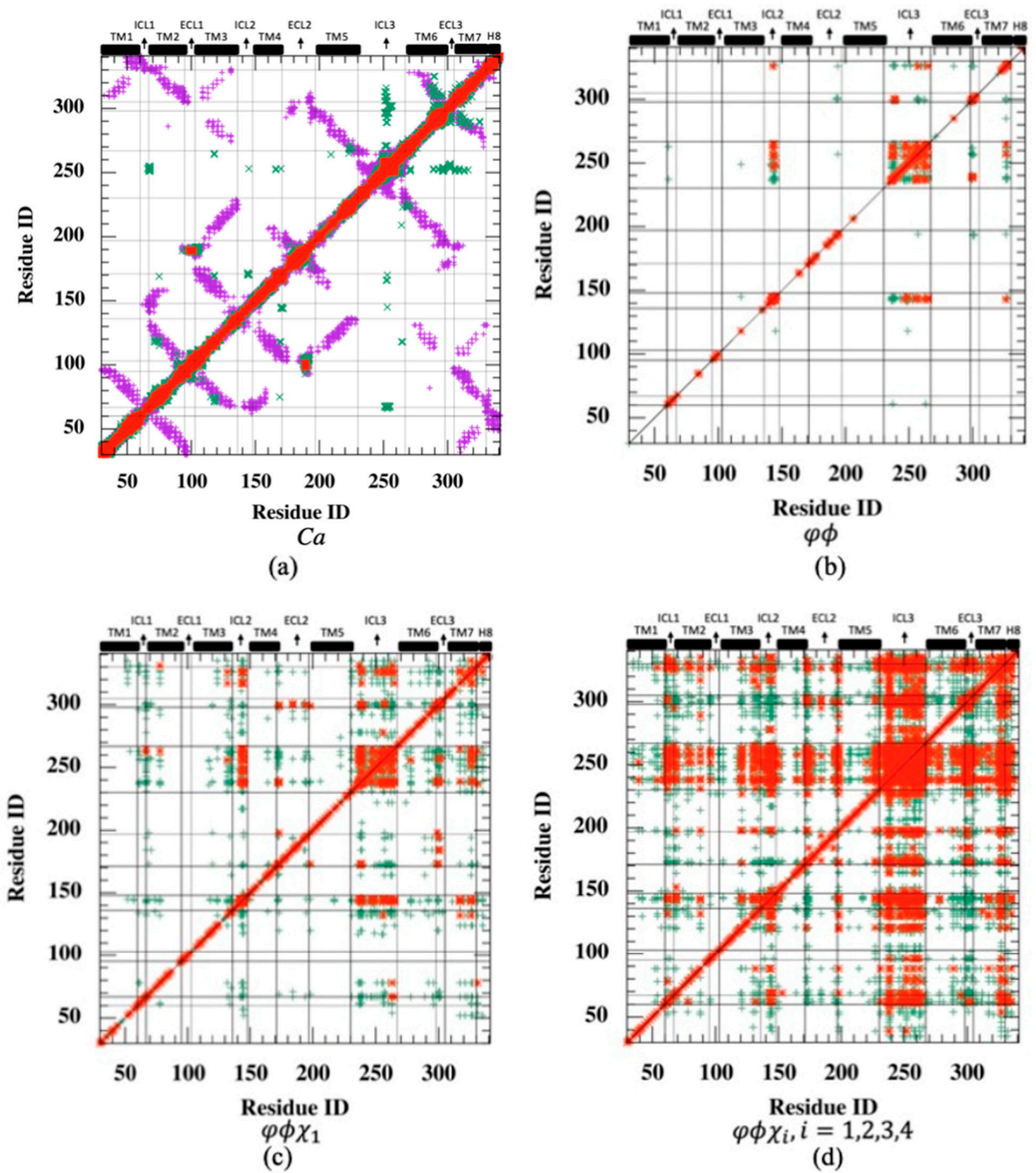


Figure 3. Cont.

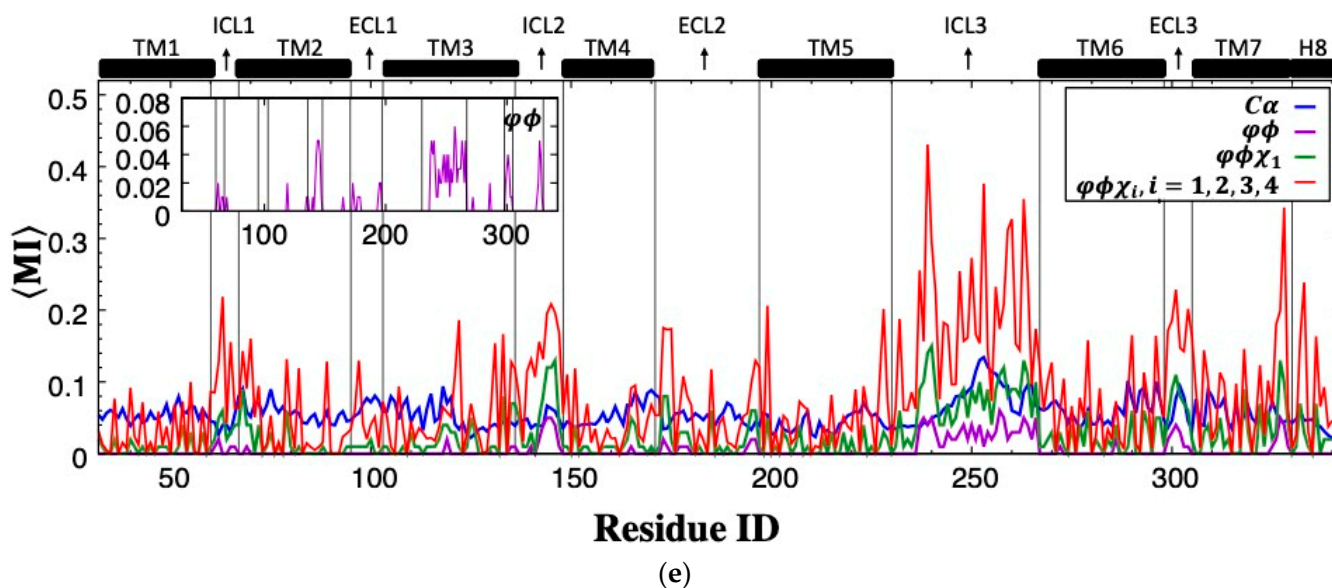


Figure 3. Residue-pair mutual information (MI) plotted with contact map (threshold: 6.0 Å) for (a) backbone $C\alpha$, (b) backbone torsion angles (ϕ , ψ) (c) backbone torsion and first side-chain torsion angles (ϕ , ψ , χ_1), (d) backbone torsion and all side-chain torsion angles (ϕ , ψ , χ_i , $i = 1, 2, 3, 4$). (e) Mean mutual information per residue averaged over the rest of the receptor. (Green dots: $0.25 < MI \leq 0.5$; red dots: $MI > 0.5$).

The residue-pair MI was next determined for backbone torsion angles ϕ and ψ in each residue. Despite low MI values observed almost everywhere in the receptor (highest MI = 2.59), the relatively high correspondence between ICL3 and ICL2 regions is noticeable (See Figure 3b). Conformational degrees of freedom were mostly dominated by torsion angles in loop regions; thus, the correspondence of loop regions was anticipated. However, the amount of such correspondence appeared to be limited to a few loop regions when only backbone torsion angles were incorporated. Hence, the next attempt was to combine the information of backbone torsion angles with that of the first side-chain torsion angle, χ_1 . Maximum MI was slightly increased to 3.72 from 2.59, and the highest MI values were still observed between ICL3 and ICL2 with increased intensity, as depicted in Figure 3c. Additionally, both ICL3 and ICL2 started to share information with the intracellular part of TM7, and moreover, two distant extracellular loop regions, ECL2 and ECL3, displayed some noticeable correspondence with each other.

The total effect of rotational degrees of freedom on MI values can only be disclosed when all possible side-chain torsion angles (χ_i , $i = 1, 2, 3, 4$) were considered together with backbone torsion angles. As illustrated in Figure 3d,e, the increasing trend in MI values between ICL3 and ICL2 was noticeable. Maximum MI reached a value of 6.55. In addition, ICL3 started to share information with the majority of the receptor, including mainly loop regions such as ICL1, ICL2 at the intracellular part, two ends of the extracellular loop ECL2, the entire ECL3, and also the intracellular part of TM7 with its adjacent tail H8. Overall, it is clear that mutual correspondence driven by torsional degrees of freedom mainly existed between loop regions.

It is important to identify residue types most often involved in sharing mutual information, especially among distal ones, as they might point to potential allosteric hub regions. Residue pairs were categorized based on the degree of separation of two residues in the primary sequence, as proximal if 1–4 positions apart and otherwise distal. As illustrated in Figure 4, the highest amount of MI was shared among polar residues, which incorporated *Arg* predominantly. Moreover, two bulky residues *Phe* and *Tyr*, with the highest MI values among hydrophobic residues, also paired with polar *Arg* to a large extent. On the other hand, no significant correspondence was observed among hydrophobic residues. The dom-

inating feature of polar residues in sharing MI can be attributed to their abundance in loop regions, which displayed a noticeably higher amount of MI than transmembrane regions in addition to their higher amount of rotational degrees of freedom. As illustrated in Figure 4c, the frequency of a residue type in loop regions is slightly proportional to its average shared MI. Almost all polar residues indicated with red dots displayed frequency values above 5%, which represents the random occurrence, whereas only three hydrophobic residues, *Gly*, *Phe* and *Leu*, had frequencies above 5%. On the other hand, two polar residues *Ser* and *Thr*, both with hydroxyl groups in their side-chains and frequency values above 7%, displayed low average MI values.

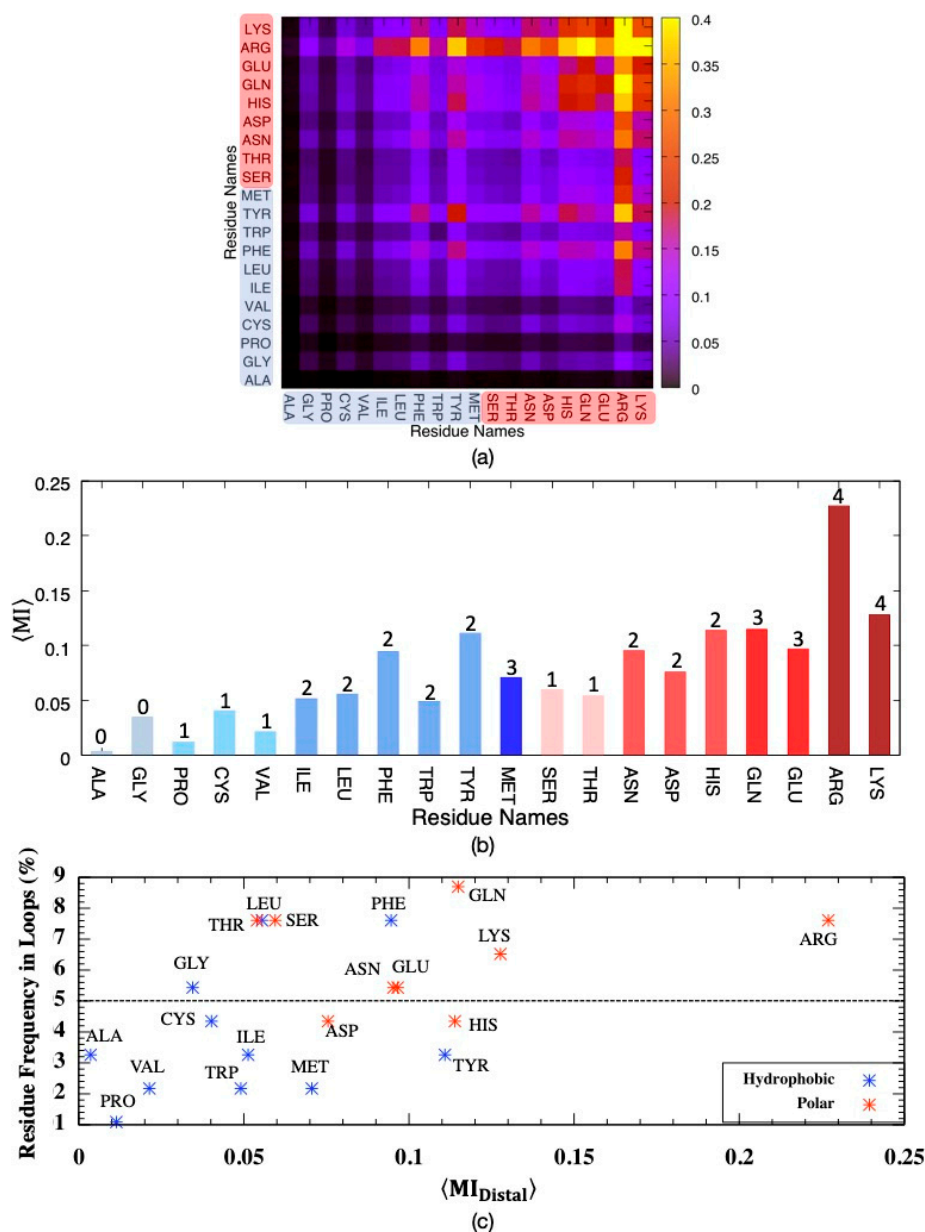


Figure 4. Mutual information for pairs of distal residues classified as either hydrophobic (blue tones) or polar (pink tones) considering all backbone (ϕ , ψ) and side-chain torsion angles (χ_k , $k = 0, 1, 2, 3, 4$), averaged over (a) residue pairs, (b) residue types with the number of side-chain torsion angles k and (c) residue frequency in loop regions versus average MI.

Interestingly, *Arg* and *Lys*, with four rotatable bonds on their positively charged side-chains, displayed slightly different average MI values with respect to each other; with an average MI of 0.23 ± 3.64 , *Arg* shared twice as much information as that of *Lys* despite the

fact that both residues were found in nearly equal amounts everywhere in the receptor ($\sim 7\%$ in loops and $\sim 3\%$ in transmembrane helices, See Supplementary Figure S1). The side-chain of *Arg* has a positively charged guanidium moiety, which favors π -stacking with aromatic rings and has the potential of forming five hydrogen bonds. As the side-chain of *Arg* protrudes from the surface of the protein, it has a crucial role in protein–protein interactions. Hence, it is not surprising to see the highest correspondence between *Arg* and the majority of residues, especially polar ones.

Mutual information is a measure of correspondence between two residues i and j with respect to their dynamic behaviors, such as positional fluctuations ($C\alpha$) or torsional changes happening at the exact same moment. Transfer entropy is another important feature that relates the dynamic states of two residues separated by a time lag parameter τ . In other words, transfer entropy measures the amount of information transferred from residue i to residue j at a later time. Knowing the state of residue i , the state of another residue j at a distant site can be predicted if there exists an allosteric communication pathway connecting the two sites. Similar to mutual information analysis, net transfer entropy was first calculated based on the backbone $C\alpha$ atom's positional fluctuations (see Equations (7) and (8) in Section 2). As depicted in Figure 5a, in one of two MD runs, the intracellular loops ICL3, ICL2, TM3, and TM4 moderately appeared as entropy donor sites, whereas the intracellular part of TM1 was detected as a dominant acceptor site. The second MD trajectory displayed a relatively different distribution profile for donor/acceptor sites; ICL3, together with the extracellular part of TM7, appeared as two dominant entropy donor sites, whereas no major acceptor site was detected (See Figure 5b). The maximum amount of information transferred was observed as 16.32 in Run#1 and 18.15 in Run#2. These results clearly indicate alternative communication pathways that can be established via positional fluctuations of $C\alpha$ atoms for the same system in two separate runs.

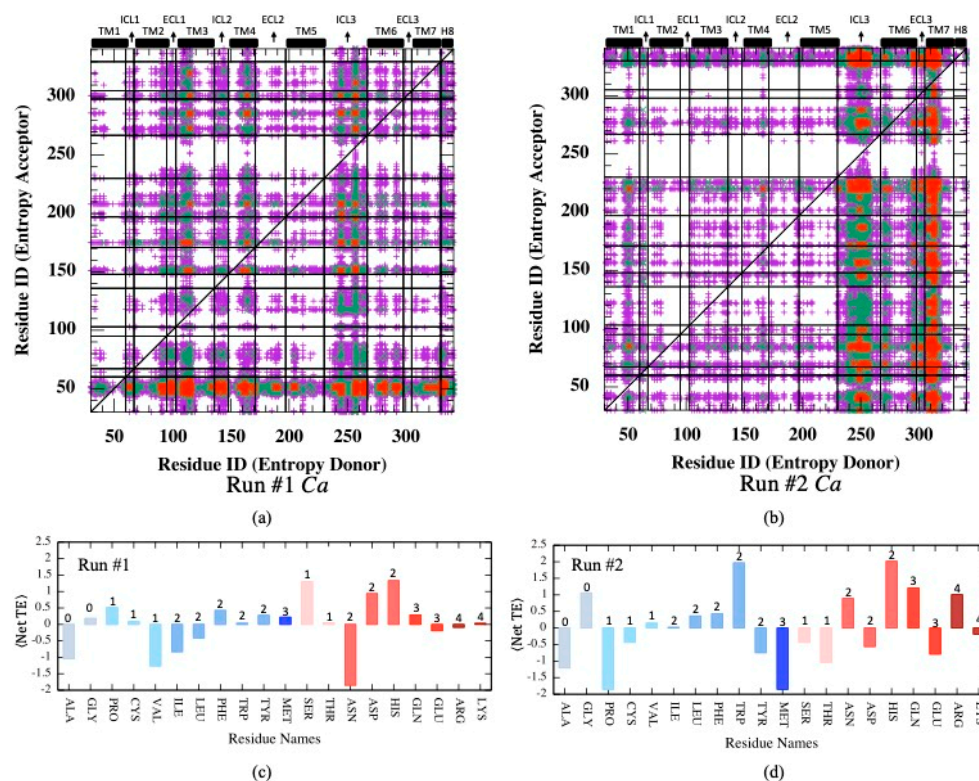


Figure 5. (a,b) Net transfer entropy from residue i to residue j (See Equation (8)) based on $C\alpha$ fluctuations for two independent MD runs. (c,d) Net transfer entropy averaged for each residue type categorized as either hydrophobic (blue tones) or polar (pink tones) and the number of side-chain torsion angles k indicated at the top of each bar. Color code for (a,b): no display for $\langle netTE \rangle \leq 4$; magenta for $4 < \langle netTE \rangle \leq 8$, green for $8 < \langle netTE \rangle \leq 12$ and red for $12 > \langle netTE \rangle$.

Furthermore, net transfer entropy was averaged for each residue type categorized as either hydrophobic or polar, as depicted in Figure 5c,d, where positive and negative $\langle netTE \rangle$ values correspond to entropy donor and acceptor residues, respectively. Clearly, no correspondence was detected between the number of side-chain torsion angles and the net entropy in both runs. In addition, there is no clear tendency for polar or hydrophobic residues to display either entropy donor or acceptor features. Furthermore, two runs displayed two completely different donor/acceptor profiles with respect to residue types. This is especially noticeable in $\langle netTE \rangle$ maps illustrated for all residue pairs, such as entropy donor versus entropy acceptor depicted in Supplementary Figure S2. Several residues displayed opposite features, e.g., entropy donor in one run and acceptor in the second run, such as *Pro, Cys, Val, Ile, Leu, Tyr, Met, Ser, Thr, Asn, Asp, Glu, and Lys*. Apparently, fluctuations in $C\alpha$ displacements were not driven by residue type, which incorporates the information of both polarity/hydrophobicity and the number of degrees of freedom.

Transfer entropy was next determined using backbone torsion angles, (φ, ψ) . As depicted in Figure 6a, ICL3 appeared as the only source of entropy donor to a few isolated acceptor regions detected on mostly loops such as ICL1, ECL1, ECL2, ECL3 and the intracellular part of TM7 adjacent to segment H8. Maximum TE values were determined as 10.86 and 11.54 for two runs, which are well below $C\alpha$ -based TE values. Next, the first side-chain torsion angle (χ_1) was considered together with two backbone angles for identifying the information of the rotameric state transferred from one residue to another in the receptor. As illustrated in Figure 6b, the same loop regions still appeared as entropy donor sites with an increased intensity dominating the future fluctuations of torsional angles everywhere in the receptor. In addition, maximum TE values reached 26.46 and 31.54 in two runs.

Unfortunately, the addition of more than one side-chain torsion angle made the computation intractable due to triple joint probability calculations (See Equation (7)), as it roughly required a memory space of 523,792,501,128 bytes ($= 3^{18} \times N_{Arg} \times N_{Lys} \times 8(\text{bytes}/\text{ArrayCell})$) only for calculating the $p(\Delta R_j(t), \Delta R_j(t - \tau), \Delta R_i(t - \tau))$ parameter of the transfer entropy equation between all *Arg* and *Lys* pairs, which exceeded the maximum amount available for today's computer technology. However, the same analysis was conducted for all possible side-chain torsion angles χ_k , $k = 1, 2, 3, 4$ only. As anticipated, information transferred from one region to another site increased significantly, with a maximum TE value reaching 61.34 for Run #1 and 63.38 for Run #2 (see Figure 6c). All intra- and extracellular loops that extended slightly towards the neighboring helices were detected as important entropy donor sites. These results clearly represent that the conformational states of the side-chains at loop regions extensively dominated the future conformational states of side-chain torsion angles everywhere in the receptor.

Finally, the net transfer entropy was further decomposed and replotted for each of the 20 residue types, as depicted in Figure 7, using a bar plot to display the average net transfer entropy where the entropy source (donor) and sink (acceptor) residues can be identified by their positive and negative values, respectively. Corresponding plots that display net transfer entropy for a pair of residue types such as entropy donor versus entropy acceptor are provided in Supplementary Figure S3. Further categorization of residues as hydrophobic and polar clearly demonstrated the dominance of polar residues as entropy donors, whereas hydrophobic ones were most often identified as entropy acceptors. In the case of backbone rotation angles only, *Trp* appeared as the strongest entropy acceptor site in both MD runs, whereas *His* displayed the highest positive average net transfer entropy (See Figure 7a). Exceptionally, *Gly* residue with no side-chain atoms appeared as a strong entropy donor site.

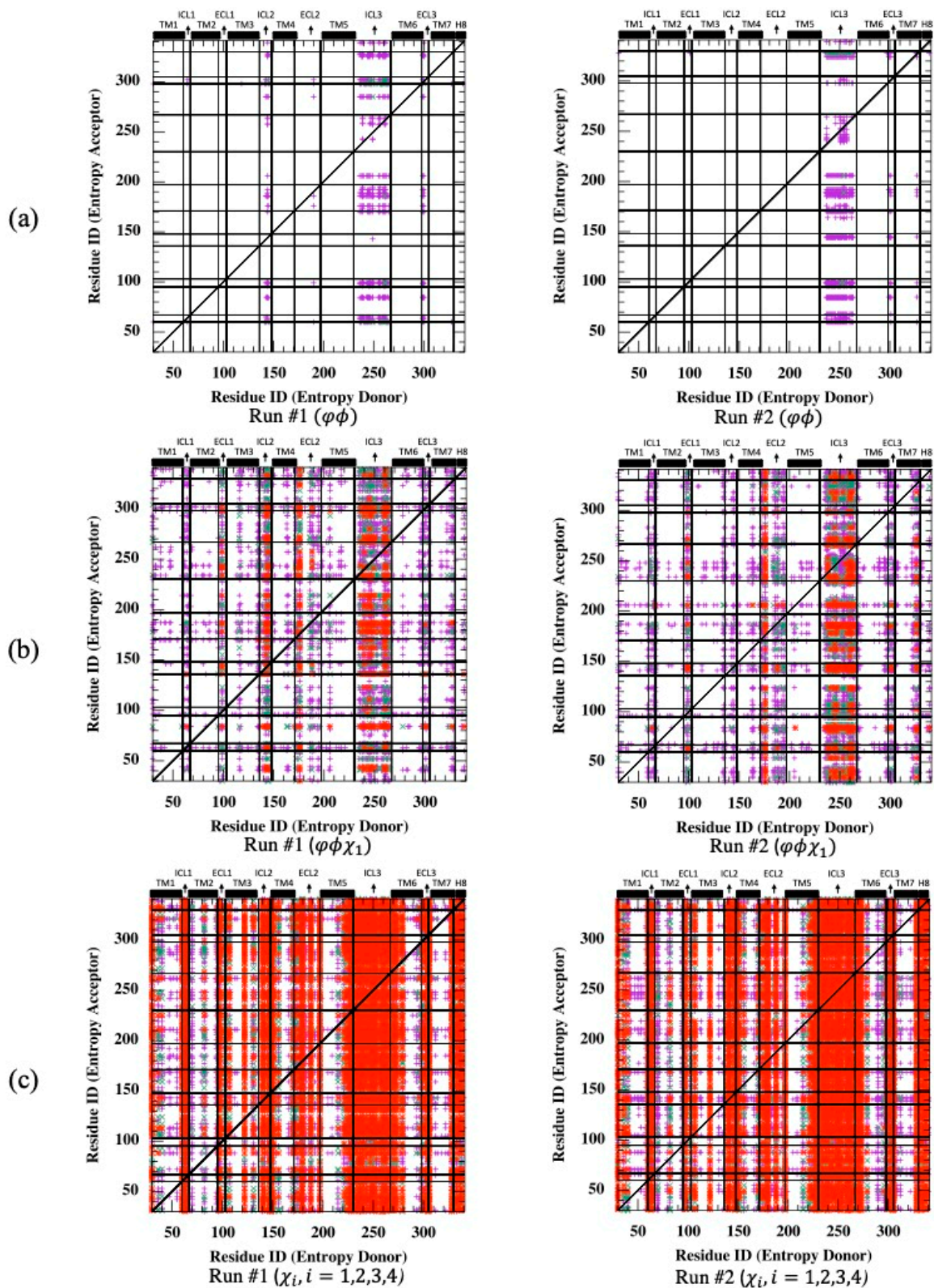


Figure 6. Net transfer entropy from residue i to residue j (see Equation (8)) for two independent MD runs using (a) backbone torsion angles, (ϕ, ψ) , (b) backbone torsion angles, (ϕ, ψ) and the first side-chain torsion angle (χ_1) and (c) all possible side-chain torsion angles $\chi_k, k = 1, 2, 3, 4$. Color code for (a,b): no display for $\langle netTE \rangle \leq 4$; magenta for $4 < \langle netTE \rangle \leq 8$, green for $8 < \langle netTE \rangle \leq 12$ and red for $12 > \langle netTE \rangle$.

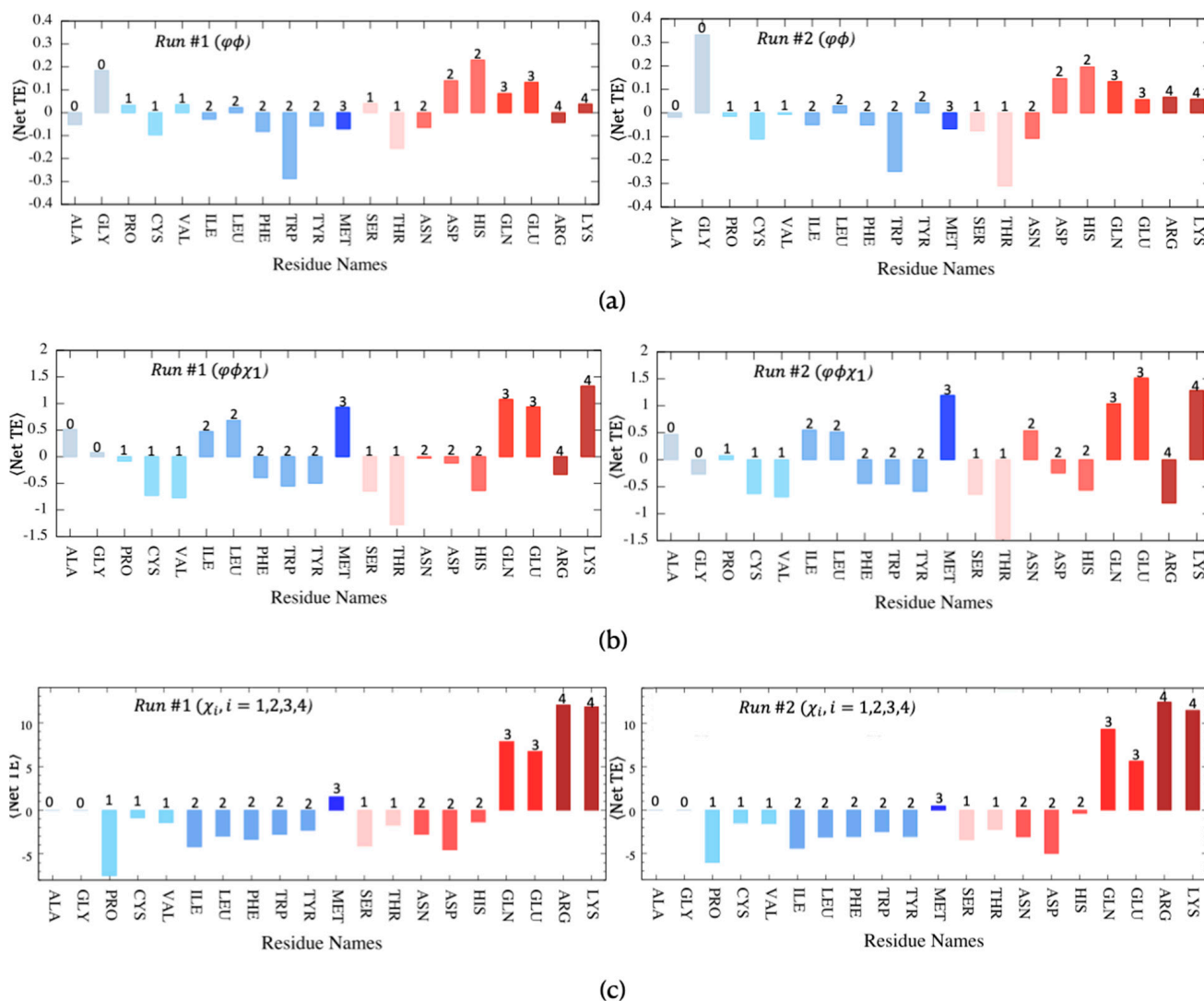


Figure 7. Net transfer entropy averaged for each residue type categorized as either hydrophobic (blue tones) or polar (pink tones). The number of side-chain torsion angles k indicated at the top of each bar is determined for both MD runs using (a) backbone torsion angles, (ϕ, ψ) , (b) backbone torsion angles, (ϕ, ψ) and the first side-chain torsion angle (χ_1) and (c) all possible side-chain torsion angles χ_k , $k = 1, 2, 3, 4$.

Noticeably, the close correspondence between polarity/hydrophobicity and donor/acceptor features was the strongest when all side-chain torsion angles were considered in transfer entropy calculations (See Figure 7c). Most hydrophobic residues, except *Met*, which is mostly located at the protein's core region, displayed strong entropy acceptor characteristics, especially *Pro*, with the lowest average net transfer entropy value of -7.38 calculated so far. Furthermore, on the polar side, *Arg* and *Lys*, with a total of four side-chain torsion angles, displayed the highest entropy values exceeding $+10$. Upon incorporating the first side-chain torsion angle (χ_1) along with two backbone torsion angles, the profile changed slightly, yet the dominance of polar residues as entropy donor sites persisted (See Figure 7b). Three polar residues, *Lys*, *Glu*, and *Gln*, displayed the highest positive transfer entropy values in both runs. Interestingly, the two polar *Ser*, *Thr*, and the hydrophobic *Tyr*, which all contain a hydroxyl group in their side-chain, displayed entropy sink (acceptor) features.

4. Conclusions

Two independent 1.5 μ s long MD simulations were conducted on the apo form of the active state of human β_2 AR in a complex with a Gs protein. Throughout both trajectories, the active state of the receptor was well preserved with the characteristic tilt in transmembrane helix 6 and ICL3 towards the lipid bilayer to give Gs full access to the binding cavity at the intracellular part. On the extracellular part, since no ligand was attached at the orthosteric site, a minor expansion was observed because of the slightly distancing motion of TM5 from TM3. However, this slight conformational shift at the extracellular part did not cause any allosteric interference in the intracellular region.

Distant regions fluctuating in the correspondence are critical as they might point to potential sites along the allosteric pathway. In this study, we attempted to use several metrics for that purpose. First, residue-pair cross-correlations were calculated for α -Carbon atomic fluctuations from average positions. Distant and correlated regions were mainly observed within the last three transmembrane helices (TM5, TM6, and TM7), including the longest loop region ICL3 and the small extension H8 adjacent to TM7. Moreover, TM6 and TM7 fluctuated in opposite directions with TM1. As cross-correlation ignores the correlated motions in orthogonal directions, the mutual information metric was next used to identify all possible distant sites in correspondence that might be critical for allosteric signaling. First, only α -Carbon atomic fluctuations were considered. However, not much correspondence was detected in the receptor except between ICL3 and the distant extracellular parts of TM6 and TM7. The next step was to replace α -Carbon fluctuations with rotameric states of backbone torsion angles ϕ and ψ in each residue when formulating the mutual correspondence. A considerable change was observed in the profile where ICL3's rotameric states fluctuated in concert and with respect to ICL2. Incorporating side-chain torsion angles further increased the mutual information transferred between ICL3 and ICL2. In addition, ICL3 started to share information with all the other loop regions, including some limited portions of transmembrane helices, TM3, TM6, and TM7.

When mutual information was further decomposed based on types of residue pairs, polar ones, especially *Arg*, were identified as the dominating group sharing the highest correspondence with other polar residues. Hydrophobic residues shared the least amount of mutual information, except *Tyr* and *Phe*, which paired with polar *Arg*. The lowest amount of MI was observed among hydrophobic residues. The dominating feature of polar residues was attributed to their higher abundance in loop regions where the highest mutual information was detected. However, despite its low abundance in loop regions, hydrophobic *Tyr* with two side-chain torsion angles had average mutual information of 0.11, which was comparable with that of other polar residues with two side-chain torsion angles.

Transfer entropy, which is another metric in information theory, relates two states at different times. If the state of residue j in the future time can be predicted knowing the state of residue i at the present time, then two sites might communicate with each other as part of an allosteric signaling network. First, transfer entropy was determined for the information about positional fluctuations ($C\alpha$). Different profiles were observed in two independent MD runs. In one run, ICL3, ICL2, TM3, and TM4 moderately appeared as entropy donor sites, whereas the intracellular part of TM1 was detected as a dominant acceptor site. In the second run, ICL3, together with the extracellular part of TM7, appeared as two dominant entropy donor sites, whereas no major acceptor site was detected. Clearly, there is no unique communication pathway for backbone $C\alpha$ displacements. When the information type was replaced by the fluctuation in the rotameric states of backbone torsion angles (ϕ , ψ), a completely different profile of communication network appeared and persisted in both runs; ICL3 was the only source of entropy donor to a few isolated acceptor regions detected mostly on loops such as ICL1, ECL1, ECL2, ECL3 and the intracellular part of TM7 adjacent to segment H8. The intensity of transferred information was relatively weak, 10.86 and 11.54 for two runs, which were well below $C\alpha$ -based TE values (16.32 and 18.15). Then, the rotameric states of the first side-chain torsion angle (χ_1) were combined with those of backbone torsion angles. As anticipated, the intensity of transferred information noticeably

increased with a maximum value of 26.46 and 31.24 in two runs. Due to computational limitations, the addition of another side-chain torsion angle was not achievable, yet the increasing trend in transfer entropy was predictable. When only the rotameric states of side-chain torsion angles were used, transfer entropy significantly increased to its highest values (61.34 and 63.38), yet the distribution profile among regions was preserved, i.e., the fluctuations of torsion angles in the loop regions drove the future fluctuations of rotameric states everywhere in the receptor. This result clearly elucidates an important aspect of all GPCRs where both extra- and intracellular loops protruding from the transmembrane bilayer play a major role in the functional regulation. Thus, loop regions can be essential targets for the design of allosteric drug molecules with fewer side effects.

Supplementary Materials: The following supporting information can be downloaded at: <https://www.mdpi.com/article/10.3390/app12178530/s1>, LIST OF SUPPLEMENTARY FIGURES: Figure S1. Residue frequency (%) of each residue type in loop and transmembrane (TM) regions. Figure S2. (a,b) Average net transfer entropy based on C α fluctuations for residue pairs classified as either hydrophobic (blue) or polar (pink) for two MD runs. Figure S3. (a,b) Average net transfer entropy for residue pairs classified as either hydrophobic (blue) or polar (pink) for two MD runs based on rotameric states of (a) backbone torsion angles, (ϕ , ψ), (b) backbone torsion angles, (ϕ , ψ) and the first side-chain torsion angle (χ_1) and (c) all possible side-chain torsion angles χ_k , $k = 1, 2, 3, 4$.

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